STOCHASTIC GRADIENT VARIATIONAL BAYES FOR DEEP LEARNING-BASED ASR

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ABSTRACT

Many successful methods for training deep neural networks (DNN) rely on an unsupervised pretraining algorithm. It is particularly effective when the number of labeled training samples is not large enough, because pretraining method helps to initialize the parameter values in the appropriate range near a local good minimum, for further discriminative finetuning. However, while the improvement is impressive, training DNN is difficult because the objective function of DNN is highly non-convex function of the parameters. To avoid placing the parameter that generalizes poorly, a robust generative modelling is necessary. This paper explore an alternative of generative modelling for pretraining DNN-based acoustic modelling using Stochastic Gradient Variational Bayes (SGVB) within autoencoder framework called Variational Bayes Autoencoder (VBAE). It performs an efficient approximate inference and learning with directed probabilistic graphical models. During fine-tuning, probabilistic encoder parameters with latent variable components are then used in discriminative training for acoustic model. Here, we investigate the performances of DNN-based acoustic model using the proposed pretrained VBAE in comparison with widely used pretraining algorithms like Restricted Boltzmann Machine (RBM) and Stacked Denoising Autoencoder (SDAE). The results reveal that VBAE pretraining with Gaussian latent variables gave the best performance.

Index Terms— acoustic model, deep neural network, variational bayes, autoencoder

1. INTRODUCTION

Automatic Speech Recognition (ASR) has changed dramatically in recent years. Previously, the standard ASR framework used Hidden Markov Model (HMM) to model the speech state transition/sequence [1] and Gaussian Mixture Model (GMM) to model each acoustic state on HMM from speech features [2]. GMMs hold such advantages as being easily fit into data using EM algorithms (especially with diagonal covariance matrix) and if they have enough parameters, they can approximate any distribution very well. However, GMMs also have disadvantages which is statistically inefficient for modelling highly correlated data due to the independent assumption of diagonal covariance. Furthermore, EM algorithms for GMM often suffer from overfitting when the component number is not adequate with the data amount.

Various state-of-the-art performances produced by deep learning have revitalized the use of various kinds of neural network architecture in ASR. A Deep Neural Network (DNN) based ASR has gained popularity in recent years, driven by bigger performance improvements than such to the previous common methods like GMM/HMM [3]. As DNNs are less sensitive to data correlation and the increase in the input dimensionality than GMMs, they allow us to exploit complex data features [4]. Many successful methods for training DNN rely on an unsupervised pretraining algorithm. It is particularly effective when the number of labeled training samples is not large enough, because pretraining method helps to initialize the parameter values in the appropriate range near a local good minimum, for further discriminative finetuning.

Therefore, the resurgence of deep learning also made generative modelling for pretraining deep neural network architecture become interesting topic to be explored. The major motivations behind generative pretraining is that if we have the good representation for modelling our data, then those representation should also be good for modelling probability class given those data [5]. There are several generative model which based on neural network and can be extended for deep neural network architecture. For example, Restricted Boltzmann Machine (RBM) [6] is an undirected graphical model with a form of Markov Random Field (MRF). Later, Deep Boltzmann Machine (DBM) [7] was invented with deeper model compared standard RBM and resulting better performance. But the main disadvantages from undirected graphical model such as RBM and DBM still exists where the exact parameter estimation is intractable and need to be approximate. Another approach for pretraining use autoencoder architecture called Stacked Denoising Autoencoder (SDAE) [8] trained by injecting some noise into input layer and minimize the reconstruction error against the clean input to help the model give better performance and robust under the corruption of input and unseen data. However, using reconstruction error is not enough for learning useful representation [9].
This paper explores an alternative of generative modelling for pretraining DNN-based acoustic modelling using Stochastic Gradient Variational Bayes (SGVB) [10] within autoencoder framework called Variational Bayes Autoencoder (VBAE). It performs an efficient approximate inference and learning with directed probabilistic models. VBAE objectives contain a regularization term, therefore regularization hyper-parameter from autoencoder model such as denoising and sparsity is not necessary anymore. During fine-tuning, probabilistic encoder parameters with latent variable components are then used in discriminative training for acoustic model. We compare the results with other widely used unsupervised pretraining algorithms for DNN, such as RBM and SDAE and purely supervised DNN-ReLU with dropout regularization.

2. RELATED WORKS

Using a Bayesian framework, we involve the prior distribution over the parameters of the component distributions. By conditioning on the observed data, the posterior distribution over the component parameters will find the best generalization over all possible values. However, true posterior distribution is intractable and we need an efficient approach for approximate the true posterior. As an alternative, the Variational Bayesian (VB) method for training GMMs acoustic model [11] and incorporated for model selection [12, 13] was explored for speech recognition. Compared with classic EMs for training GMMs, VB estimation provides information about the model quality during training and is less affected by overfitting because of the regularization from integrating priors.

Variational inference was first considered for neural network by Alex Graves [14] as an optimization of the Minimum Description Length (MDL) [15] loss function to optimize the prediction accuracy and the model complexity at the same time. This study performs Bayesian inference on neural network which estimates directly the posterior distribution of the network weights given the observed data. Therefore, the weights from neural networks have a prior probability which acts as regularization from a variational perspective.

Recently, SGVB was proposed to learn generative model with latent variables using neural network [10]. It combines both concepts of variational inference and neural network into a single framework. Since it consists of probabilistic encoder and decoder for approximate the latent variable distribution, this model was known as VBAE. It has been explored for modelling image transformation, in which SGVB was applied to CNN architecture, and the model learns an interpretable representation of images with respect to rotation and lighting variations [16]. In addition to a generative model, SGVB can also be used for semi-supervised learning [17] using the variational autoencoder to generate latent variables as features for a classifier or by jointly modelling datasets with class and latent variables as a generative model.

To the best of our knowledge, SGVB-VBAE has not been explored for ASR tasks. In this preliminary study, however, instead of applying VBAE directly as feature generator, we attempt to utilize it for pretraining DNN-based acoustic modelling. This way we could learn a good representation for modelling our data and that representation can be integrated for discriminative task in ASR.

3. VARIATIONAL BAYES AUTOENCODER FOR GENERATIVE MODEL

Variational Bayes Autoencoder (VBAE) is an alternative for performing efficient approximate inference and learning with directed probabilistic models [10]. With Stochastic Gradient Variational Bayes (SGVB) algorithm, the parameters for approximate posterior was effectively learned end-to-end without using such an expensive sampling method as Markov Chain Monte Carlo (MCMC). Typically, we have dataset \( X = \{x^{(i)}\}_{i=1}^N \) with \( N \) samples where \( x^i \in \mathbb{R}^D \), which are observable variables. We assume the data are generated under some random process involving by a latent continuous random variable \( z \). Value \( z^{(i)} \) which corresponds to data \( x^{(i)} \), is generated from prior distribution \( p_{\theta^*}(z) \), and value \( x^{(i)} \) is generated from conditional distribution \( p_{\theta^*}(x|z) \). To simplify the problem, we assume prior \( p_{\theta^*}(z) \) and likelihood \( p_{\theta^*}(x|z) \) come from the parametric families of distribution \( p_0(z) \) and \( p_0(x|z) \) whose PDFs can be optimised w.r.t. both parameter \( \theta^* \) and latent variables \( z^{(i)} \) need to be approximated. Several limitations such as the intractability of the integral of the marginal likelihood towards all possible latent \( z \) values \( p_0(x) = \int p_0(x|z)p_0(z)dz \) and sampling based solutions like Monte Carlo would be too slow for large datasets.

To overcome these limitation, we used approximate distribution \( q(z|x) \) for modelling true posterior \( p_0(z|x) \). In VBAE, neural network was used for approximate distribution \( q(z|x) \) and called as a probabilistic encoder. In a similar term as probabilistic encoder, the value \( z \) would be used for reconstruct input with conditional distribution \( p_0(x|z) \) as a probabilistic decoder. Using same approach as probabilistic encoder above, \( p_0(x|z) \) computed from \( z \) by using a neural network.

The marginal likelihood from individual datapoints can be represented by the sum of the log marginal likelihood:

\[
\log p_0(x^{(1)}, \ldots, x^{(N)}) = \sum_{i=1}^N \log p_0(x^{(i)}),
\]

and the marginal likelihood for each datapoint \( x^{(i)} \) can be
simplified into two terms:

\[
\log p_\theta(x^{(i)}) = D_{KL}(q_\phi(z|x^{(i)})||p_\theta(z|x^{(i)})) + L(\theta, \phi; x^{(i)}),
\]

(2)

where the left term is written as the KL-divergence between the approximate and true posterior distributions and is non-negative and the right term denotes the variational lower bound to the marginal likelihood, which can be expanded

\[
\log p_\theta(x^{(i)}) \geq \mathcal{L}(\theta, \phi; x^{(i)}) = \mathbb{E}_{q_\phi(z|x)}[-\log q_\phi(z|x) + \log p_\theta(x, z)] = -D_{KL}(q_\phi(z|x^{(i)})||p_\theta(z)) + \mathbb{E}_{q_\phi(z|x^{(i)})}[\log p_\theta(x^{(i)}|z)].
\]

(3)

By maximizing lower bound \(\mathcal{L}(\theta, \phi; x^{(i)})\) w.r.t parameters \(\theta\) and \(\phi\), we can build good approximation for our dataset \(\log p(x^{(i)})\). In VBAE, the approximate posterior (probabilistic encoder) \(q_\phi(z|x)\) is represented by a DNN. For example, if we are using approximate Gaussian with diagonal covariance \(q_\phi(z|x^{(i)}) = \mathcal{N}(z; \mu^{(i)}, \sigma^{(i)} I)\), mean \(\mu^{(i)}\) and s.d. \(\sigma^{(i)}\) are outputs from DNN.

4. UTILIZING VBAE FOR ACOUSTIC MODELS

Standard dataset \(D = \{x^{(i)}, y^{(i)}\}_{i=0}^N\) consists of a pair of context window of consecutive feature vectors and acoustic labels/states. First, we do unsupervised training for the VBAE to maximize marginal likelihood \(\log p(x^{(i)})\). The feature vectors are usually represented by the transformed speech signals by standard feature extraction for acoustic features like MFCC, Fourier-based filterbank and fMLLR. Those feature extractions output real values. In this case, we must reparameterize our probabilistic decoder to output Gaussian parameters such as vector of mean \(\mu_{dec}\) and diagonal s.d \(\sigma_{dec}\):

\[
\log p_\theta(x|z) = \log \mathcal{N}(x; \mu_{dec}, \sigma_{dec}^2 I) \quad \mu_{dec} = f_{linear}(W_{\mu_{dec}} h_2 + b_{\mu_{dec}})
\]

\[
\log \sigma_{dec} = f_{linear}(W_{\sigma_{dec}} h_2 + b_{\sigma_{dec}})
\]

\[
h_2 = f_{tanh}(W_2 h_z + b_2).
\]

With same approach as the probabilistic decoder, the probabilistic encoder parameters can be computed by DNN from \(z^{(i)}\). We use Gaussian distribution to approximate posterior distribution \(q_\phi(z|x)\), so we need to reparameterize the probabilistic encoder to output Gaussian parameters \(\mu_{enc}\) and \(\sigma_{enc}\):

\[
z = \mu_{enc} + \sigma_{enc} \odot \epsilon \quad \text{where} \quad \epsilon \sim \mathcal{N}(0, I)
\]

\[
\mu_{enc} = f_{linear}(W_{\mu_{enc}} h_1 + b_{\mu_{enc}})
\]

\[
\log \sigma_{enc} = f_{linear}(W_{\sigma_{enc}} h_1 + b_{\sigma_{enc}})
\]

\[
h_1 = f_{tanh}(W_1 x + b_1).
\]
the latent variable \( z \) from \( q(z|x) \) which conditionally sampled from \( \mu_{enc} \) and \( \sigma_{enc} \) as features for a classifier or integrating the entire probabilistic encoder with pretrained parameter and add another DNN with softmax layer on the top of \( \mu_{enc} \) and \( \sigma_{enc} \). Fig. 2 illustrates how we constructed a discriminative DNN using VBAE’s pretrained probabilistic encoder for extracting latent variable and end-to-end fine-tuning from the negative log-likelihood loss function from the softmax layer. This stage which is usually called as discriminative fine-tuning, is generally done for classification tasks by several unsupervised pretraining algorithms such as RBM and SDAE.

5. EXPERIMENTAL SETUP

5.1. Dataset

All the phoneme recognition experiments were performed on the TIMIT corpus dataset. All the SA records were removed from the experiment. The training set contains 3696 sentences from 462 speakers. Development set was taken from another 50 sets of speakers. Evaluation was done by evaluating our model into core test set that consisted of 192 sentences from 24 different speakers.

5.2. Front-End

In this experiment, we used speaker adapted fMLLR features to represent speech signals, which were obtained using a GMM-HMM model built by Kaldi [20] s5 TIMIT recipe for tri3 scenario. Every acoustic frame was represented by 40 features. We used five context windows expanded to the left and right. We combined 11 consecutive acoustic frames combined 440 features per time frame. With the tri3 scenario, the acoustic model states consisted of 1946 tied triphone states, and for decoding we used the phoneme bigram language model, which was estimated from the training set for decoding purposes.

5.3. Baseline Systems

5.3.1. RBM

Our RBM experiments were done using the KaldiPDNN toolkit [21, 22]. For a baseline RBM experiment, we used a Gaussian-Bernoulli RBM to model our continuous data features from the input layer. Then we stacked multiple Bernoulli-Bernoulli RBM on top of the previous hidden layer and pretrained the layers one by one from the bottom to the top. We used four hidden layers, each of which contains 1024 hidden units. In the end, we put a softmax layer with 1946 units to represent class probability and fine-tuned it using negative log-likelihood cost function.

5.3.2. SDAE

Our SDAE experiments were done using the KaldiPDNN toolkit. For our baseline SDAE experiment, we use tanh nonlinearity to reconstruct input from the hidden layer. We use four hidden layers, each of which contains 1024 hidden units, which is same as the baseline RBM number of hidden layers and unit size. In the end, we put a softmax layer with 1946 units represent class probability and fine-tuned it using negative log-likelihood cost function.

5.3.3. DNN-ReLU + Dropout

In this baseline experiment, we used supervised DNN with rectifier linear activation function and dropout regularization [23]. Identical as before, we also constructed four hidden layers with rectifier linear activation function with 1024 units for each layer. We tried several dropout probabilities for each layer between 0.2 and 0.5 and selected the best model from development set for the baseline DNN-ReLU+Dropout.

5.4. VBAE-DNN Experiment

For the VBAE experiment, we first built two layers of 1024 hidden units for modelling our probabilistic encoder and 2 layer of 1024 hidden unit for modelling our probabilistic decoder. In this experiment, we tried several different numbers

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1. http://www.ldc.upenn.edu/Catalog/CatalogEntry.jsp?catalogId=LDC93S1
of latent variables within 64, 128, and 256 with \( L = 1 \) for each datapoint.

After the generative model training was finished, we used the pretrained probabilistic encoder parameter and projected the unit mean and unit diagonal covariance into one hidden layer and put softmax layer on the top. In the end, we have four hidden layers with 1024-1024-[128,256,512]-1024 units for VBAE-DNN. We also compared two different scenarios, (1) without using dropout, (2) use dropout only at last hidden layer before softmax layer. For the second scenario, we used dropout probability 0.25 for the last hidden layer.

6. EXPERIMENT RESULTS

Table 1 compares the performances from various models in terms of phoneme error rates (PER (%)) on the TIMIT core test set. First, the RBM baseline result was 21.1% PER and the SDAE baseline result was 21.6% PER. We also experimented on standard DNN ReLU + dropout and trained it without unsupervised pretraining and the result was 20.4% PER.

Next we performed an experiment described in section 4 and varied the number of latent variables. The best performance for VBAE without dropout regularization was obtained both by 64 and 128 latent variables with 20.6% PER. For the second scenario, by using dropout on the last hidden layer, we improved the recognition performance for both the VBAE with 64 and 128 latent variables to 19.8% PER.

Table 1. Comparison of all experiments in terms of phoneme error rates (PER) on TIMIT core test set

<table>
<thead>
<tr>
<th>Model</th>
<th>Test PER (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>RBM</td>
<td>21.1</td>
</tr>
<tr>
<td>SDAE</td>
<td>21.6</td>
</tr>
<tr>
<td>DNN-ReLU+DO</td>
<td>20.4</td>
</tr>
<tr>
<td>VBAE (256-latent)</td>
<td>20.9</td>
</tr>
<tr>
<td>VBAE (128-latent)</td>
<td>20.6</td>
</tr>
<tr>
<td>VBAE (64-latent)</td>
<td>20.6</td>
</tr>
<tr>
<td>VBAE+DO (256-latent)</td>
<td>20.0</td>
</tr>
<tr>
<td>VBAE+DO (128-latent)</td>
<td>19.8</td>
</tr>
<tr>
<td>VBAE+DO (64-latent)</td>
<td>19.8</td>
</tr>
</tbody>
</table>

7. CONCLUSION

This paper explored the use of VBAE trained by SGVB algorithm for generative pretraining deep neural networks. Our results reveal that pretrained parameters from a probabilistic encoder of VBAE can produce a better results in comparison with another generative pretraining algorithms with similar neural network configurations. The best accuracy was obtained by 64 and 128 Gaussian latent variable VBAE models with 20.6% PER, and we achieved 19.8% PER with dropout regularization.

In the future, we will further investigate the use of SGVB in various different NN architecture such as Convolutional Neural Network (CNN) and Recurrent Neural Network (RNN) to improve ASR performance. The possibility to utilize SGVB as a feature generator for GMM acoustic model will also be explored. Furthermore, we would be interested to investigate the robustness of this approach for low resources problems in speech recognition.

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